

## Review Problems for Differential Equations

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$$1. \quad xy y' - 2y^2 + 2x^2 = 0.$$

$$2. \quad y' - y^2 \sin^2 x = x^2 y^2.$$

$$3. \quad \left(e^{x^2} + e^{y^2}\right) y y' + e^{x^2} (xy^2 - x) = 0.$$

$$4. \quad y' \cos^2 x + 3y - 1 = 0.$$

$$5. \quad 3x \cos y - y' e^{-3x} \sin y + \cos y = 0.$$

$$6. \quad -2y^3 + 3xy^2 y' - x^3 e^{2x} = 0.$$

$$7. \quad y'' - 2y' - 8y = e^{-2x}.$$

$$8. \quad y'' + 4y' + 7y = 5x.$$

$$9. \quad y'' - y' - 20y = \sin 3x.$$

$$10. \quad y^2 y' - xy' - y + x^2 = 0$$

$$11. \quad xy' - 2y - x^2 = 0$$

$$12. \quad 2xy' + xy^3 - y = 0$$

$$13. \quad 2x^2 y' - y^2 - 2xy - 3x^2 = 0$$

$$14. \quad xyy' - 2yy' - 3xy^2 - x = 0$$

**15.**  $y' \tan y + x^2 y' \sec^2 y + 2x \tan y + \sec^2 x = 0$

**16.**  $y'' - 4y' + 9y = x$

**17.**  $y'' - 10y' + 25y = 3$

**18.**  $y'' + 4y' + 3y = e^{-x}$

**19.**  $y' - 2xy = 3x$

**20.**  $(x^3 + 8) y' - x^2 \cos^2 y = 0$

**21.**  $2x \ln y + \frac{x^2 y'}{y} + \frac{y'}{y^2 + 3} = 0$

**22.**  $xy' - 2y = x^4 \cos x$

**23.**  $x^4 - 2xy^2 + x^2yy' = 0$

**24.**  $x^2y' - y^2 - xy + 4x^2 = 0$

**25.**  $y'' + y' + y = \sin 2x$

**26.**  $y'' - y' - 12y = e^{-3x}$

**27.**  $y' - 5x^2 - x^2y^2 = 0.$

**28.**  $3xyy' - 4y^2 + xy + 2x^2 = 0$

**29.**  $\sin 3x + 5e^{5x} \sin y^2 + 2yy'e^{5x} \cos y^2 + y' \sec 4y = 0$

**30.**  $(x^2 + 6)y' + 8xy - 4x = 0.$

**31.**  $e^x \cos y - y'e^{-3x} \sin y + \cos y = 0.$

**32.**  $x^2 + y^4 - xy^3y' = 0.$

**33.**  $y'' - 2y' - 15y = e^{-3x}.$

**34.**  $y'' + 6y' + 14y = 6x + 2.$

**35.**  $y'' - 6y' + 13y = xe^{-x}$

**36.**  $xy' - 3y = x^4e^{2x}$

**37.**  $y'' - 8y' + 16y = x^2$

**38.**  $\frac{-2y}{x^3} - \sin^2 x + \frac{y'}{x^2} + yy' = 0$

**39.**  $x^2y' - y^2 - xy - 4x^2 = 0$

**40.**  $yy' + xyy' + y^2 + 5 = 0$

**41.**  $xy' + y' + 3y + x = 0$

**42.**  $y^4y' + x^2yy' + xy^2 + \frac{1}{x} = 0$

**43.**  $y'' + 4y' + 10y = e^{3x}$

**44.**  $y'' - 6y' + 8y = e^{-5x}$

$$\mathbf{45.} \quad y'' + 2y' + y = \sin 2x$$

$$\mathbf{46.} \quad y' + y \tan x = \sec x$$

$$\mathbf{47.} \quad ye^{x^2}y' + \frac{y'}{y} + xy^2e^{x^2} + 2x^3 = 0$$

$$\mathbf{48.} \quad y'' - 2y' + 3y = 2x$$

$$\mathbf{49.} \quad y'' - 4y' + 4y = e^{-3x}$$

$$\mathbf{50.} \quad e^{x^2}y' + xy^2 + 2x = 0$$

$$\mathbf{51.} \quad 3e^{3x} \cos 2y + \tan 2x - 2y'e^{3x} \sin 2y = 0$$

$$\mathbf{52.} \quad yy' + 4xyy' - y^2 - 1 = 0$$

$$\mathbf{53.} \quad xy' - 5y - x^2 = 0$$

$$\mathbf{54.} \quad y'' - 6y' + 8y = xe^{2x}$$