

# Math 373 Hw 5 Recommended problems, don't turn this in.

Hw 156: 4.68, 4.70. 166: 4.90, 4.92. 189: 5.4, 5.6, 5.8, 5.12. Rec. 156: 4.69, 4.71. 166: 4.86, 4.95. 189: 5.5, 5.7, 5.13.

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4.69 A worker-operated machine produces a defective item with probability .01 if the worker follows the machine's operating instructions exactly, and with probability .03 if he does not. If the worker follows the instructions 90% of the time, what proportion of the items will be defective?

4.71 A particular football team is known to run 30% of its plays to the left and 70% to the right. When a play goes to the right their right guard shifts his stance most of the time (80%) and uses a balanced stance the remainder of the time. When plays go to the left, the guard takes a balanced stance 90% of the time and a shift stance the remaining 10%. On a particular play, the right guard takes a balanced stance.

- (a) Find the probability that the play will go to the left?
- (b) Find the probability the play will go to the right?
- (c) If you were a linebacker for the opposing team, which direction would you prepare to defend if you saw the guard take a balanced stance?

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4.86 A piece of electronic equipment contains six computer chips, two of which are defective. A subset of three chips is selected at random, removed from the piece of equipment, and inspected. Let  $x$  equal the number of defectives observed, where  $x = 0, 1, \text{ or } 2$ . Find the probability distribution for  $x$ . Give the probability distribution table for  $x$ .

4.95 From experience, a shipping company knows that the cost of delivering a small package within 24 hours is \$14.50. The company charges \$15.50 for shipment but guarantees to refund the charge if delivery is not made within 24 hours. If the company fails to deliver only 2% of its packages within 24 hours, what is the expected gain per package?

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5.5 In a binomial distribution for a random variable  $x$ ,  $n = 6$  and  $p = .8$ . Construct a probability distribution table for  $x$ .

5.7 Let  $x$  be a binomial random variable with  $n = 10$  and  $p = .4$ . Find

- (a)  $P(x=4)$
- (b)  $P(x \geq 4)$
- (c)  $P(x > 4)$
- (d)  $P(x \leq 4)$
- (e)  $\mu$
- (f)  $\sigma$

5.13 Find the mean and standard deviation for a binomial distribution with the given values.

- (a)  $p = .01$
- (b)  $p = .0$
- (c)  $p = .3$
- (d)  $p = .7$
- (e)  $p = .5$

## Answers

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4.69 **.012**

4.71

- (a) Go to the left? **.66**
- (b) Go to the right? **.34**
- (c) Which direction? **left**

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4.86

$x$	0	1	2
$p(x)$	0.2	0.6	0.2

4.95 **69¢**

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5.5 In a binomial distribution for a random variable  $x$ ,  $n = 6$  and  $p = .8$ . Construct a probability histogram  $x$ .

$x$	0	1	2	3	4	5	6
$p(x)$	0	0.002	0.015	0.082	0.246	0.393	0.262

5.7 Let  $x$  be a binomial random variable with  $n = 10$  and  $p = .4$ . Find

- (a)  $P(x=4) = .251$
- (b)  $P(x \geq 4) = .681$
- (c)  $P(x > 4) = .367$
- (d)  $P(x \leq 4) = .633$
- (e)  $\mu = 4$
- (f)  $\sigma = 1.55$

5.13 Find the mean and standard deviation for a binomial distribution with the given values.

- (a)  $p = .01$        $\mu = 1$      $\sigma = .99$
- (b)  $p = .9$          $\mu = 9$       $\sigma = 3$
- (c)  $p = .3$          $\mu = 30$      $\sigma = 4.58$
- (d)  $p = .7$          $\mu = 70$      $\sigma = 4.58$
- (e)  $p = .5$          $\mu = 50$      $\sigma = 5$