

Page 336. Write acceptance regions in the format below:

$$x \in 10 \pm (1.96)(.5) = [9.02, 10.98]$$

$$\text{or } \bar{x} \in [10 - (1.645)(.5), \infty) = [9.18, \infty)$$

$$\text{or } \bar{x} \in (-\infty, 10 + (1.645)(.5)] = (-\infty, 10.83]$$

9.4(5). A random sample of  $n=35$  observations from a quantitative population produces a mean of  $\bar{x}=2.4$  with std. dev.  $s=.29$ . Suppose your research objective is to show, at the 5% significance level, that the population mean  $\mu$  exceeds 2.3.

$$H_a: \mu > 2.3, \quad H_0: \mu \leq 2.3, \quad \text{hence } \mu_0 = 2.3.$$

(a) Find the null region (include variable  $\mu$ ).

Find the acceptance region (write in both forms, include  $\bar{x}$ ).

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(b) Suppose the alternate value is  $\mu_a=2.4$ . Find the probability  $\beta$  of falsely accepting  $H_0$ .

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(c) Same as (b) but with alternate value  $\mu_a=2.5$ .

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(c') Same as (b) but with alternate value  $\mu_a=2.6$ .

. . . .

(e) As the distance between  $\mu_0$  and  $\mu_a$  increases what happens to value of  $\beta$ ?

increases? decreases?

9.11'(7). A drug manufacturer claims that one of its drugs has an average potency of 70%. A random sample of  $n = 100$  capsules are tested and found to have a sample mean of  $\bar{x} = 68\%$  with std. dev.  $s = .8\%$ . You wish the level of significance to be 5%.

(a)  $\mu_0 =$  \_\_\_\_\_  $H_0:$  \_\_\_\_\_  $H_a:$  \_\_\_\_\_

(b)  $SE =$  \_\_\_\_\_ %  $z_{\alpha/2} =$  \_\_\_\_\_  
 $SE = \sqrt{\frac{pq}{n}}$  or  $\frac{\sigma}{\sqrt{n}}$ ?

(c) Find the null region.

Find the acceptance region (both forms with 4-place decimals, e.g., .5831 for 58.31%).

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(d) What is the  $p$ -value of the sample mean  $x = 68\%$ ?

(e) Do the data present sufficient evidence to refute the manufacturer's claim at the 5% significance level?

(f)(2) If the alternate value is  $\mu_a=66\%$ , find  $\beta$ .

As part of the calculation of  $\beta$ , draw a picture like that of the lecture. Correctly picture  $\mu_a \in (-\infty, a_1]$ , or  $\in [a_1, a_2]$  or  $\in [a_2, \infty)$