Math 411
HOMEWORK \#3
Due Wednesday, Feb. 5, 2014

1. Let $V$ be the vector space of $2 \times 2$ matrices over the field $F$.
a. Prove that $V$ has dimension 4 by exhibiting a basis of four elements.
b. Let $W_{1}$ be the set of matrices of the form $\left(\begin{array}{cc}x & -x \\ y & z\end{array}\right)$ and let $W_{2}$ be the set of matrices of the form $\left(\begin{array}{cc}a & b \\ -a & c\end{array}\right)$. Prove that $W_{1}$ and $W_{2}$ are subspaces of $V$.
c. Find the dimensions of $W_{1}, W_{2}, W_{1}+W_{2}$ and $W_{1} \cap W_{2}$.
2. Page 48, \#4
3. Page $52, \# 6$.
